

Name: .....

Student ID: .....

1. [12 p.] What is chaos in the context of nonlinear dynamics?
2. [12 p.] What are the Feigenbaum constants?
3. [12 p.] Explain the idea behind construction of a fractal.
4. [12 p.] Sketch a 1-D phase portrait corresponding to the following system:

$$\dot{x} = \sin x. \quad (1)$$

5. [13 p.] Determine if the following system is linear or nonlinear:

$$\ddot{x} + \dot{x} + \sin x = 0. \quad (2)$$

6. [13 p.] Linearise the following system:

$$\begin{cases} \dot{x} = -y, \\ \dot{y} = y(x^3 + y^3) + x. \end{cases} \quad (3)$$

7. [13 p.] **Video:** (Link: [https://www.youtube.com/watch?v=TYXVgJdcX\\_Q](https://www.youtube.com/watch?v=TYXVgJdcX_Q)) Is the magnetic pendulum shown in the video and in Fig.1 a chaotic system? If you believe the pendulum to be chaotic, then what is the source or sources of the chaos?
8. [13 p.] **Video:** Does the pendulum have an unstable fixed point (unstable pendulum position)? If so, can we position the pendulum at that point for a prolonged period of time? Explain your answers.

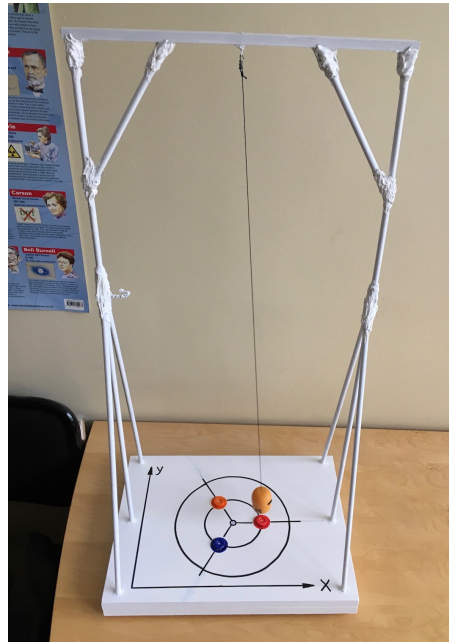


Figure 1: The magnetic pendulum in three magnetic potentials relevant to Questions 7 and 8. The magnets are marked with the red, orange and blue colours.