VHDL-AMS

VHDL-AMS - Analog & Mixed Signal extensions


Superset of VHDL - IEEE Standard 1076-1993

Can be used to model electrical or mechanical systems

Mathematical Foundation
Equations describing continuous parts are differential-algebraic equations (DAEs)
DAE theory has been developed in the last 15 years
Theory covers properties and the numerical solution of DAEs of the form
\( F(x,\frac{dx}{dt},t)=0 \) where \( x \) is the vector of unknowns and \( F \) is a vector of expressions

Reasons for development
Need for only one simulator as they are expensive
Support for modeling level above Spice
The growth of mixed signal systems
Pure VHDL Model of Differentiator

```vhdl
entity diff is
    generic (r, c: real);
    port (vi: in real; vo: out real);
end entity diff;

architecture simple of diff is
begin
    process (vi) is
        variable tnow, tlast: real;
    begin
        tnow := real(now/ns)*1.0e-9;
        vo <= -R*C(vi - vi'last_value)/(tnow - tlast);
        tlast := tnow;
    end process;
end architecture simple;
```

Unidirectional signals. Does not support Kirchoff’s law.

Connects time to real and control time step. The problem is event driven nature.

Write own formulae.
Quantities and Equations

• Two New Objects for VHDL
  – Terminal
    • Either interface object or local object
    • Terminal associations create analog netlists
      \textbf{terminal} t1,t2:electrical;
  
• Two New Objects for VHDL
  – Quantities
    • Either interface object or local object
    • Quantity associations create \textit{signal flow} models
      \textbf{quantity} a,b,c: voltage;

quantity\_declaration::= \text{free\_quantity\_declaration} \\
| branch\_quantity\_declaration \\
| source\_quantity\_declaration

free\_quantity\_declaration::= \\
quantity identifier\_list : subtype\_indication [:= expression] ;
Implicit Quantities

- **Q’Dot**  The time derivative of quantity Q
- **Q’Integ**  The integral of Q from 0 to current time
- **Q’Delayed(t)**  The quantity Q at time NOW-t
- **S’Ramp[(tr[,tf])]**  A scalar quantity of the same type as signal S, that follows S with specified rise and fall times
- **S’Slew[(max_rising_slope [,max_falling_slope])]**  Similar to S’Ramp, but with maximum slopes
- **Q’Slew[(max_rising_slope,[max_falling_slope])]**  A scalar quantity that follows Q but with maximum slopes
- **Q’ZOH(T,[initial_delay])**  Zero-order hold with specified sampling interval and first sampling time
- **Q’Ltf(num,den)**  Laplace transfer function of Q (scalar)
- **Q’Ztf(num,den,T [, initial_delay])**  Z-domain transfer function of Q (Scalar) with specified sampling interval
Branch Quantities

branch_quantity_declaration ::= quantity [across_aspect] [through_aspect] terminal_aspect;
across_aspect ::= identifier_list [tolerance_aspect] [:= expression] across
through_aspect ::= identifier_list [tolerance_aspect] [:= expression] through
terminal_aspect ::= plus_terminal_name [to minus_terminal_name];

• Defines a named flow path or a named effort difference; for example current and voltage
• Declared with a plus terminal and minus terminal
  quantity v across j,i through t1 to t2;
• Plus terminal and minus terminal must have the same simple nature
• Minus terminals default to “ground”
• A branch quantity is composite if one of the terminals is composite
• Implicit quantity T’Reference is an across quantity directed from T to “ground”
• Implicit quantity T’Contribution is the signed sum of through quantities incident to T
Terminals and Natures

- Terminals belong to a nature
  
  Terminal_declaration::= terminal identifier_list : subnature_indication ;

- Two terminals may enter into a terminal association
  
  port map ( anode => t1, cathode => t2);

- A locally declared terminal or an unassociated formal terminal is the root terminal of a node

nature_declaration ::= nature identifier is nature_definition
nature_definition ::= scalar_nature_definition | composite_nature_definition
scalar_nature_definition ::= type_mark across type_mark through
subnature_declaration ::= subnature identifier is subnature_indication

- Terminals may be associated only with terminals of like nature
- Across aspect represents effort-like effects -- voltage, temperature, pressure
- Through aspect represents flow-like effects -- current, heat flow rate, fluid flow rate
- N’reference is a terminal - the “ground” for all terminals with nature N
Example: Package for electrical systems

```vhdl-ams
package electrical_system is
    subtype voltage is real;
    subtype current is real;
    subtype charge is real;
    subtype flux is real;

    nature electrical is voltage across current through;
    nature electrical_vector is array(natural range <>) of electrical;

    alias ground is electrical'reference;
end package electrical_system;
```
Source Quantities

source_quantity_declaration ::= 
    quantity identifier_list : subtype_indication source_aspect;

source_aspect ::= 
    spectrum magnitude_simple_expression, phase_simple_expression 
    | noise magnitude_simple_expression

function FREQUENCY return real;

- Source Quantities specify small-signal stimulus
  - Spectral source quantity for AC simulation
  - Noise source quantity for small-signal noise simulation

- Magnitude and phase expressions may depend on quantities and FREQUENCY
Implicit DAEs

- Each Across quantity is the difference between reference quantities of its terminals
- The algebraic sum of through quantities at a root terminal is zero
- The reference quantities of each pair of associated terminals are equal
- Each pair of associated terminals are equal
- Each implicit quantity is constrained to its appropriate value
Simultaneous Statements

- Simultaneous Statements express explicit DAEs
  
simultaneous_statement ::= simple_simultaneous_statement
  | simultaneous_if_statement
  | simultaneous_case_statement
  | simultaneous_procedural_statement
  | simultaneous_null_statement

- The semantics of if, case and procedural are derived from the semantics of the simple simultaneous statement

- The Simple Simultaneous Statement
  - Simultaneous statement has a collection of characteristic expressions
    
simple_simultaneous_expression ::= 
    [label:] simple_expression ==
    simple_expression [tolerance_aspect];
Simultaneous Statements

- **Scalar expressions:**
  - The statement has a single characteristic expression - the difference of the statement expressions

- **Composite expressions:**
  - There must be a matching scalar subelement of the right-hand expression for each scalar subelement of the left-hand expression
  - The characteristic expressions are the differences of the matching scalar subelements of the statement expressions

- **The Simultaneous Conditional Statement**
  - Selects one of the enclosed sequences of simultaneous statements

\[
\text{simultaneous\_if\_statement ::=}
\]

\[
\begin{align*}
\text{[if\_label:]} & \quad \textbf{if} \; \text{condition} \; \textbf{use} \; \text{simultaneous\_statement\_part} \\
\text{[ elsif} \; \text{condition} \; \textbf{use} \; & \text{simultaneous\_statement\_part]} \\
\text{[ else} \; & \text{simultaneous\_statement\_part]} \\
\text{end use [if\_label];}
\end{align*}
\]
Simultaneous Statement

• The Simultaneous Case Statement
  – Selects one of a number of alternative simultaneous statement lists

 simulatenous_case_statement ::= 
  [case_label:] case expression use
  simultaneous_alternatives
  end use [case_label];

 simulatenous_alternative ::= 
  when choices => simultaneous_statement_part

• The Simultaneous Procedural Statement
  – Allows the formulation of equation as in-line sequential code

 simulatenous_procedural_statement ::= 
  [procedural_label:] procedural [is]
  procedural_declarative_part
  begin
  sequential_statements
  end procedural [procedural_label];
Simultaneous Statement

- Semantics of Simultaneous Procedural Statement
  - Defined by rewrite to the form:
    \[ FP(T'_{a}(Q_1,..Q_m),X_1,..X_n) \equiv T'_{a}(Q_1,..Q_m) \]
  - The Qs are quantities, the Xs are quantities, signals, constants or literals
  - FP contains local variable declarations corresponding with, and initialized to, the values of Q1..Qm
  - The members of Q1..Qm are just those variables that are “written” by sequential statements
  - FP returns the aggregate of the values of those variables
Examples of Simultaneous Statements

• A linear resistor

```
use electrical_system.all;
entity resistor is
    generic (resistance: real);
    port (terminal n1, n2: electrical);
end entity resistor;

architecture signal_flow of resistor is
    quantity vr across ir through n1 to n2;
begin
    ir == vr / resistance;
end architecture signal_flow;
```
Examples of Simultaneous Statements

- A parameterized diode

```vhdl
use electrical_system.all, ieee.math_real.all;
entity diode is
    generic (Iss, n, Vt, tau, Rs, Cj0, Vj: real);
    port (terminal a, c: electrical);
end entity diode;
architecture level0 of diode is
    quantity vdiode across idiode, icap through a to c;
    quantity q: charge;
    quantity nsf: real noise sqrt(idiode/frequency);
begin
    idiode == iss * (exp((vdiode-Rs*idiode)/(n*Vt))-1)+nsf;
    q == tau * idiode - 2.0*Cj0*sqrt(Vj**2-Vj*vdiode);
    icap == q'dot;
end architecture level0;
```
Examples of Simultaneous Statements

- A sinusoid voltage source

```vhdl
use electrical_systems.all, ieee.math_real.all;
entity vsource is
  generic (magnitude, freq: real;
            phase: real := 0.0);
  port (terminal a, c: electrical);
end entity vsource;

architecture sine of vsource is
  quantity v across i through a to c;
  quantity ac:real spectrum magnitude/sqrt(2.0),phase;
begin
  v == magnitude * sin(2.0*math_pi*freq*NOW) + ac;
end architecture sine;
```
Tolerances

• Each quantity and simultaneous statement belongs to a user-definable tolerance group, which can be specified for subtypes, subnatures, quantities and simultaneous statements
  
  subtype_indication ::= [resolution_function_name] type_mark [constraint] [tolerance_aspect]
  
  tolerance_aspect ::= tolerance string_expression
  
  subnature_indication ::= nature_mark [index_constraint]

  [tolerance string_expression across string_expression through]

• The tolerance group of a quantity is specified by its subtype
  - The “closest” tolerance aspect found when tracing subtype (or subnature) indications back to the base type
  - The tolerance group of type real is indicated by “”

• The tolerance group of a simple simultaneous statement is
  - The tolerance group of the quantity if the statement is of the form
    
    quantity_name == simple_expression;
    simple_expression == quantity_name;
  - Can be specified explicitly
Tolerance Example

• In package electrical_system:
  
  `subtype voltage is real tolerance "low_voltage";
  subtype current is real tolerance "low_current";

• In a design entity:

  `architecture two of resistor is
    quantity vr across it through n1 to n2;
    -- tolerance group of vr and ir defined by their subtype
    quantity power:real;
    -- default tolerance for power is empty string
    begin
      ir == vr/resistance;  -- default tolerance group from ir
      power == vr * ir tolerance "other";
    end architecture two;`
Time

- New Time for Mixed-Mode Simulation
  - The internal simulation time is redefined to be of a new definitional type Universal_Time
  - Conversion from Time or Real to Universal_Time is exact
  - Conversion from Universal_Time to Time and Real
    - Have identical slopes and intercepts
    - Are linear within the accuracy of the representation of Real and the resolution limit of Time
    - Always round down to the nearest Real or Time value

- Overloaded function NOW:
  impure function NOW return Real;

- Overloaded S’Last_event to return type Real
Time

- Allow Real expression in timeout clause of a wait statement:
  
  ```vhdl
  wait for 0.5;
  ```

  this is equivalent to

  ```vhdl
  quantity q: Real; signal s: Real;
  q == now-s’Ramp;
  process begin
    s<=now;
    wait for 0 ns;
    wait on q’above(0.5);
    ...
  end process;
  ```
Implicit Quantities

- S’Ramp[(tr[,tf])]  
  A scalar quantity of the same type as signal S, that follows S with specified rise and fall times

- S’Slew[(max_rising_slope [,max_falling_slope])]  
  Similar to S’Ramp, but with maximum slopes

- Q’Above(E)  
  - Implicit Boolean Signal  
  - TRUE when Q is above the threshold E and FALSE when Q is below the threshold  
  - Q must be a scalar quantity, E must be an expression of the same type as Q  
  - The transition between the two states creates an event on the signal  
  - The value may be read in any non-static expression  
  - The event may be used to trigger process execution
entity comparator is
  port (terminal n1, n2: electrical;
       signal s:out bit);
end entity comparator;

architecture ideal of comparator is
  quantity v across n1 to n2;
begin
  with v’Above(0.0) select
    s <=
      ‘1’ when true,
      ‘0’ when false;
end architecture ideal;
Simulation Cycle

• How does the simulation cycle work?
  – Analog simulation cycle must deteriorate into digital one in the limits
  – Analog simulation cycle based on Universal “Real” time

• Analog simulation cycle
  a) Execute Analog Solver
  b) Set Tc=Tn, terminate if Tn $\Leftrightarrow$ Time’High or no active drivers
  c) Update active explicit signals
  d) If DOMAIN’Event, switch to time domain equations
  f) Resume processes
  g) Execute resumed nonpostponed processes
  h) Determine Tn
  i) If DOMAIN = INITIALIZATION_DOMAIN and Tn > 0 reset Tn to 0 and set the
driver of DOMAIN to
  • TIME_DOMAIN if a time domain simulation follows
  • FREQUENCY_DOMAIN if a frequency domain simulation follows
  j) Execute resumed postponed processes if Tn $\neq$ Tc
Discontinuous Models

- An abstract model may display discontinuities in its quantities as its DAEs change with time.
- Any of the following may, but does not always, cause a discontinuity when used in a simultaneous statement:
  - An event on a signal
  - A conditional test on quantities
  - A function call
- NO implicit mechanism can be designed to efficiently and automatically detect every discontinuity without introducing phantoms.
- An active break signal cues the analog solver to “process” the discontinuity.
- The values of the ASP are the initial values for the next continuous interval.
Synchronizing Analog to Digital

- A break statement announces a discontinuity in some quantity or its derivative at the instance of execution.
- Tells analog solver to reinitialize for next continuous interval.
- Both sequential and concurrent forms.
- New initial conditions may be specified at the same time.
- A model that causes a discontinuity at some time T and does not execute a break statement at T is erroneous.

```vhdl
with din select reff <=
    rof when 'Z';
    ron when others;
break on reff;
```
Synchronizing Digital to Analog

```vhdl
case s is
when 1 =>
    dout := '1';
    wait on vin’above(vlow);
when 2 =>
    dout := '0';
    wait on vin’above(vlow), vin’above(vhi);
```

- Q'above(E) is an attribute of Q.
- Q must be a scalar quantity. The result is a Boolean signal.
- An event occurs at the instance of threshold crossing.
Example: Single-pole double-throw switch

entity double_throw is
  port(
    signal control: IN bit;
    terminal p1, m1, p2, m2: electrical);
end entity double_throw;

architecture ideal of double_throw is
  quantity v1 across i1 through p1 to m1;
  quantity v2 across i2 through p2 to m2;
begin
  if control = '0' use
    i1 == 0.0; i2 == 0.0;
  else
    v1 == 0.0; v2 == 0.0;
  end use;
  break on control; -- concurrent break statement
end architecture ideal;
Example: Bouncing Ball

entity bouncer is end entity bouncer;
architecture ball of bouncer is
  quantity v:velocity; -- m/sec
  quantity s:displacement; -- m
  constant g: real := 9.81; -- m/sec**2
  constant air_res : real := 0.001; -- 1/m
begin
  s’Dot == v;
  if v>0.0 use
    v’Dot == -g - v**2*air_res;
  else
    v’Dot == -g + v**2*air_res;
  end use;
break v => -v when not s’Above(0.0); -- Announce discontinuity, reset velocity value

break v => 0.0, s => 10.0; -- Specify initial conditions
end architecture ball;
Frequency Domain Simulation

- Small signal-model defined as first term of Taylor expansion of $F(x)$ about quiescent point
- AC Simulation
  - Find quiescent point
  - Set simulation frequency
  - Replace base set of CEs with CEs defined by small-signal model
  - Augment small-signal model with frequency domain augmentation set
  - Solve resulting (linear) equations
- Noise Simulation
  - Find quiescent point
  - Set simulation frequency
  - Replace base set of CEs with CEs defined by small-signal model
  - Augment small-signal model with noise augmentation set
  - Create a noise variable corresponding to each quantity
  - For each noise source quantity NQ
    - Replace corresponding CE by NQ - magnitude
    - Solve resulting (linear) equations
    - Add to each noise variable the square of the magnitude of the corresponding quantity
    - Restore CE
  - Set each quantity to square root of corresponding noise variable
• Special definitions for mixed netlists

• A designer cannot simply “connect” a quantity port with a terminal or vice-versa, nor a quantity port with a signal

• Simultaneous statements defining the intended connection must be explicitly specified, for example

```vhdl
terminal t:electrical;
quantity v across i through t; -- branch to ground
quantity q: voltage;
component foo is
    port(quantity iq:out voltage); -- quantity “drives” terminal
end component foo;

c1: foo port map( iq => q);
v == q; -- ideal connection
```