

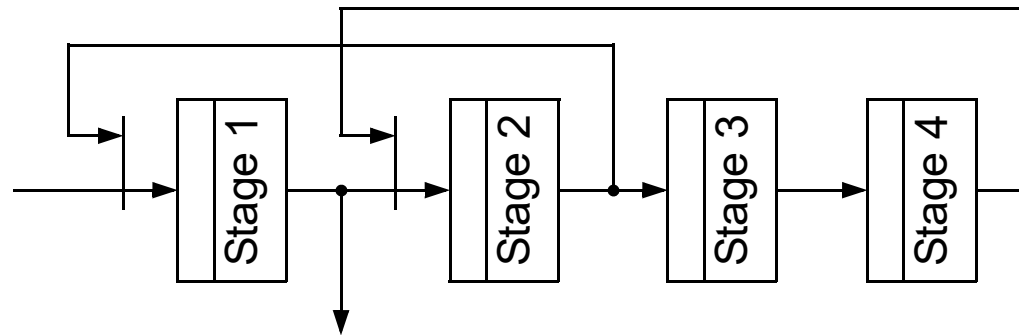
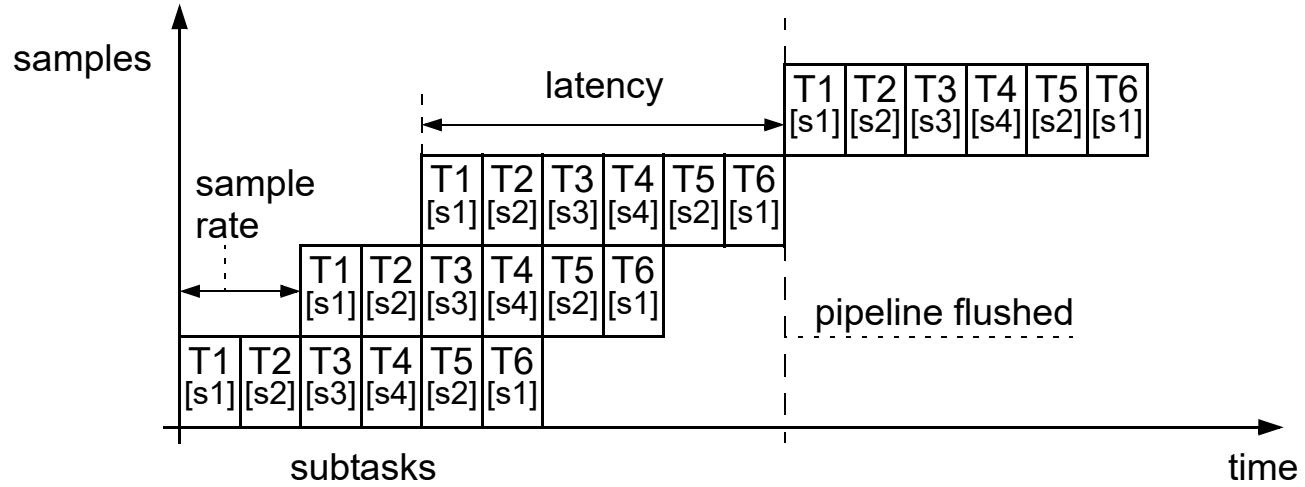


Pipelining

- ***Pipelining*** - an implementation technique whereby multiple instructions are overlapped in execution
- ***Latency (L)*** - total number of time units needed to complete the computation on one input sample
- ***Sample rate (R)*** - the number of time units between two consecutive initiations, where initiation is the start of a computation on an input sample
- ***A (pipe) stage*** is a piece of HW that is capable of executing certain subtask of the computation
- ***The reservation table*** is a two-dimensional representation of the data flow during one computation. One dimension corresponds to the stages, and the other dimension corresponds to time units.
- **Actions in pipeline: *flushing, refilling, stalling.***



Pipeline - example





Pipeline measurements

- **Average initiation rate (measure of pipeline performance):**

$$R_{\text{init}, N \rightarrow \infty} = 1 / (R \times t_{\text{stage}} + r_{\text{synchro}} \times (L-R) \times t_{\text{stage}})$$

- **R** – sample rate, **L** – latency,
- **t_{stage}** – the time one stage needs to complete its subtask,
- **r_{synchro} = N_{flush} / N** – resynchronization rate,
- **N_{flush}** – the number of input samples that cause flushing,
- **N** – number of input samples.

Functional pipelining

- **In conventional pipelining, stages have physical equivalents, i.e. the stage hardware is either shared completely in different time units or not shared at all.**
- **In the case of large functional units, there is no physical stage corresponding to the logical grouping of operations in a time step.**
- **A *control step* corresponds to a group of time steps that overlap in time. Operations belonging to different control steps may share functional units without conflict.**
- **Operations, belonging to the time steps $s+n \times L$, for $n \geq 0$, are executed simultaneously and cannot share hardware.**



Functional pipelining of 8-point FIR filter

